

USING SOFTWARE AND MATHEMATICAL METHODS TO OPTIMISE A BOTTLING FLOW

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Abstract: Automating processes has emerged as a significant global trend within the bottling industry, with a rising number of companies now focusing on this aspect. The present study conducted a simulation to optimise a bottling flow using the WITNESS Horizon software. The main objective of increasing the profit was achieved by optimising the bottling flow by modifying working times and implementing two new bottling lines. In addition, another efficient method was presented, which was solved using Kuhn's algorithm to optimise the proposed flow. The system designed in the present study was compared to other systems in the bottling industry market. The research found that the system proposed in this paper was the most efficient as it could complete a whole cycle of bottling and packing ten boxes in a shorter time than the other systems.

Keywords: automation, bottling flow, simulation, algorithm, optimisation.

1. INTRODUCTION

The general structure of a production flow consists of more than one type of system, the most important ones being: supply, transportation, transfer, packaging, labelling, palletising and storing systems.

As detailed in the paper, the bottling production flow consists of the following components: the bottling and fastening system for bottle caps, the labelling system, the belt conveyor transportation system, the storing system, and human operators.

In this case, the transportation systems are the conveyors, which take and move the bottles towards the areas where different procedures will take place (bottling, labelling, capping, palletising, wrapping, etc.) [1].

The purpose of the transfer system is to transfer the products to different stages within the bottling flow.

The storage spaces are used to store the raw materials utilised during the production flow and temporarily store the finished products.

The human operators are meant to oversee and intervene during the production flow processes if needed [1].

A bottling flow will be simulated using WITNESS Horizon to optimise the flow and achieve the highest number of finished products in the shortest amount of time.

2. COMPARATIVE ANALYSIS OF FLOW CHOICES PROVIDED BY COMPANIES WORKING IN THE FIELD

The Shemesh Automation sparkling water bottling line is fully automatic and offers a complete filling, cap fastening, labelling and sealing process using state-ofthe-art systems. This line is a complete solution that carries out the sparkling water bottling process with minimal loss.

The scheme ensures a higher effectiveness for the systems used and is meant to bottle 3000 bottles per hour [2].

The cap fixing system is designed to offer effective and precise cover for a wide array of products. The machine is built to screw caps and is fully automated for maximum efficiency.

The sealing system provides a new perspective on the quality of the sealing process and allows the making of a completely sealed product with no scraps caused by the process.



Fig. 1. Shemesh Automation bottling line [2].

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The labelling system has the perfect solution for applying different types of labels on a wide range of container shapes. This machinery is capable of applying any type of self-adhesive label. The system ensures that every label will be placed in exactly the same place on each bottle. Production never stops replacing an old labelling tape with a new one because it keeps on rolling labels as the old tape connects to the new one in order to have no breaks.

The conveyor is designed to carry both filled and empty bottles. It is equipped with an adjustable side rail for guidance, making the machine compatible with different types of bottles. It can also be adjusted in height [2].

The Krones sparkling water bottling line has an increased productivity of over 15.000 bottles per hour with a controlled filling level, and it is designed to maintain a low cost of energy and resources [3].

The bottling line is used for different types and sizes of bottles and is one of the best-performing systems when it comes to the filling method.

The Krones filling system bottles drinks with high precision while ensuring a high-quality filling process.

The cap fixing system processes a large number of caps that are fastened on bottles using a manufacturing device that is more productive.

The labelling system consists of three main components and seven types of labelling stations. It is effective and reliable equipment that allows for increased productivity.

The packaging system is automated and can handle a wide range of bottle sizes. One perk of the automated system is that it allows great flexibility regarding bottles' shapes and sizes.

The palletising system is efficient and allows fully automated loading and emptying of pallets.

The conveyor system is flexible in handling different types of bottles and maintains a constant flow, with a high enough speed and a buffer zone that is mandatory for every filling line. It is also highly effective in handling products, making very little noise and consuming little energy. The exit area is also very versatile in terms of product types, as it is equipped with high-accuracy sensors that provide smart production management.

The solutions provided by the two companies working in the bottling domain have increased productivity and can be used as templates for the devised model.



Fig. 2. Krones bottling line [3].



Fig. 3. Depicting the flow components in Witness [4].

3. SIMULATING THE PROPOSED BOTTLING FLOW USING THE WITNESS HORIZON

The following components were integrated within the simulated bottling flow: buffers, conveyors (C1, C2, C3, C4, C5, C6), the bottling system, the cap fixing system, the labelling system, the packing system, and the palletising system (Fig. 3).

Simulations have been made for the following types of bottles: 0.5 litres, 1.0 litres, 1.5 litres, 2.0 litres, and 2.5 litres PETs. The results in the paper at hand are presented for the most favourable case, which is bottling in 1.5 litre PET bottles.

Empty 1.5 litres PET bottles are taken from the buffer using a robot and transferred to the conveyor(C1) which transports them to the bottling system. After sterilisation and filling, the bottles exit the conveyor(C2) and are carried to the cap fixing system. After screwing the caps, the bottles are unloaded to the conveyor(C3) and moved to the labelling system. After applying labels, the bottles are taken by the conveyor(C4) and transported to the packing-in-cases system. The cases are picked up by the conveyor (C5) and taken to the palletising system. After finishing the palletising and wrapping processes, the pallets are moved to the deposit using the forklift.

3.1. Initial simulation and costs

The modelled systems were simulated for 5 working days (5 days x 8 hours x 60 minutes = 2400 minutes) to make a diagnosis and identify the bottlenecks (Fig. 4).

At the end of the 5-day simulation, the productivity report shown in Fig. 5 was achieved. By reviewing this report, it can be observed that 4.801 1.5-litre bottles were bottled, grouped in 794 cases, and positioned on 12 pallets, with 64 cases on each pallet.



bottlenecks.

| Name | No. Entered | No. Shipped | No. Scrapped | No. Assembled | No. Rejected | W.I.P. | Avg W.I.P. | Avg Time | Sigma Rating |
|--------------|----------------|----------------|-----------------|------------------|-----------------|-----------|------------|----------|-----------------|
| Dopuri | 12000 | 0.000 | 0.000 | 4789.000 | 0.000 | 7211.000 | 3611.282 | 722.256 | 6.00 |
| Etichete | 12000 | 0.000 | 0.000 | 4779.000 | 0.000 | 7221.000 | 3621.335 | 724.267 | 6.00 |
| Folie | 12000 | 0.000 | 0.000 | 794.000 | 0.000 | 11206.000 | 5606.507 | 1121.301 | 6.00 |
| Palet | 4801 | 0.000 | 0.000 | 12.000 | 0.000 | 4789.000 | 2394.848 | 1197.175 | 6.00 |
| Sticla_cu | 4789 | 0.000 | 0.000 | 4779.000 | 0.000 | 10.000 | 10.053 | 5.038 | 6.00 |
| Sticla_etic | 4779 | 0.000 | 0.000 | 4764.000 | 0.000 | 15.000 | 15.209 | 7.638 | 6.00 |
| Sticle | 4801 | 0.000 | 0.000 | 4789.000 | 0.000 | 12.000 | 11.282 | 5.640 | 6.00 |
| Bax | 794 | 0.000 | 0.000 | 768.000 | 0.000 | 26.000 | 32.262 | 97.516 | 6.00 |
| Produs_finit | 12 | 12.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.028 | 5.500 | 6.00 |
| | | | | | | | | | |

Fig. 5. Product report.

The analysis of the report on loading the production systems within the flow, presented in Figs. 6 and 7, shows that the palletising system has a very low loading, being inactive for 98% of the time.

Furthermore, following the analysis of the report for loading conveyors, shown in Figs. 8 and 9, it can be observed that the working time for conveyor 6 is very little, accounting for 2.5% in relation to the functioning time of the flow components. These flaws are going to be fixed as a result of adapting and optimising the flow [5].

Reports on product quantity, loading the systems in the flow and production costs were produced after simulating the initial flow.

Further, the goal is to optimise the bottling flow by improving productivity, loading the flow systems as much as possible in relation to the maximum capacity, without bottlenecks in other areas of the flow, and achieving the lowest possible production costs considering the entry benchmarks [6].

| | Name | % Idle | % Busy | % Filling | % Emptying | % Blocked | % Cycle Wait Labor |
|--|-------------|--------|--------|-----------|------------|-----------|-----------------------|
| | Imbuteliere | 82.011 | 17.989 | 0.000 | 0.000 | 0.000 | 0.000 |
| | Dopuire | 80.046 | 19.954 | 0.000 | 0.000 | 0.000 | 0.000 |
| | Etichetare | 0.425 | 99.575 | 0.000 | 0.000 | 0.000 | 0.000 |
| | Ambalare | 83.458 | 16.542 | 0.000 | 0.000 | 0.000 | 0.000 |
| | Paletizare | 98.500 | 1.500 | 0.000 | 0.000 | 0.000 | 0.000 |
| | Transport | 99.750 | 0.250 | 0.000 | 0.000 | 0.000 | 0.000 |
| | Robot | 80.000 | 20.000 | 0.000 | 0.000 | 0.000 | 0.000 |

Fig. 6. Production systems report.



| Name | % Empty | % Move | % Blocked | % Queue | % Broken Down | Now On | Total On | Avg Size | Avg Time |
|------|---------|--------|-----------|---------|------------------|--------|----------|----------|----------|
| C1 | 0.004 | 99.996 | 0.000 | 0.000 | 0.000 | 3 | 4800 | 3.513 | 1.756 |
| C2 | 0.083 | 99.917 | 0.000 | 0.000 | 0.000 | 8 | 4797 | 7.190 | 3.597 |
| C3 | 0.237 | 78.515 | 0.000 | 21.247 | 0.000 | 9 | 4789 | 9.057 | 4.539 |
| C4 | 0.445 | 94.263 | 0.000 | 5.292 | 0.000 | 12 | 4779 | 11.701 | 5.876 |
| C5 | 33.841 | 66.142 | 0.000 | 0.017 | 0.000 | 1 | 794 | 0.661 | 1.999 |
| C6 | 97.500 | 2.500 | 0.000 | 0.000 | 0.000 | 0 | 12 | 0.025 | 5.000 |

Fig. 8. Conveyor transport systems report.



Fig. 9. Conveyor chart.

Regarding costs, after reviewing the reports derived from the simulation using the initial parametrisation, the profit resulted in \$11,704.90. Considering that the profit can be increased, measures for optimising the bottling line in this sense will also be taken (Fig. 10).

3.2. Optimising the system

To meet the requirements set after simulating the initial flow, the next step was remodelling the bottling flow following the values of the initial simulation. Two more bottling lines were added to allow increasing the number of bottled, packed, and palletised bottles.

This change has taken place because, following the initial simulation, the palletising system had a much too low loading compared to the other components of the flow.

The redesigned bottling flow was reintroduced in WITNESS Horizon (Fig. 11) and properly parametrised as to achieve optimised results during the simulation [7].

A number of reports presented further below resulted from simulating and optimising the flow.



Fig. 10. Costs report.



Fig. 11. Redesigned bottling flow: *a* – optimised flow-bottling; *b* – optimised flow-packing.

| Name | No. Entered | No. Shipped | No. Scrapped | No. Assembled | No. Rejected | W.I.P. | Avg W.I.P. | Avg Time | Sigma Rating | Chart |
|--------------|----------------|----------------|-----------------|------------------|-----------------|-----------|------------|----------|-----------------|----------------|
| Dopuri | 12000 | 0.000 | 0.000 | 11993.000 | 0.000 | 7.000 | 7.431 | 1.486 | 6.000 | Chart State |
| Bichete | 12000 | 0.000 | 0.000 | 11987.000 | 0.000 | 13.000 | 13.443 | 2.689 | 6.000 | Chart Row |
| Folle | 12000 | 0.000 | 0.000 | 1997.000 | 0.000 | 10003.000 | 5003.737 | 1000.747 | 6.000 | |
| Bax02 | 1948 | 0.000 | 0.000 | 1942.000 | 0.000 | 6.000 | 14.441 | 17,792 | 6.000 | Print |
| Palet | 4801 | 0.000 | 0.000 | 44.000 | 0.000 | 4757.000 | 2378.696 | 1189.100 | 6.000 | Minitah |
| Sticla_cu | 11993 | 0.000 | 0.000 | 11987.000 | 0.000 | 6.000 | 6.012 | 1.203 | 6.000 | |
| Folie02 | 12000 | 0.000 | 0.000 | 1948.000 | 0.000 | 10052.000 | 5028.047 | 1005.609 | 6.000 | Swap rows |
| Sticla_etic | 11987 | 0.000 | 0.000 | 11982.000 | 0.000 | 5.000 | 6.482 | 1.298 | 6.000 | columns |
| Sticle | 12000 | 0.000 | 0.000 | 11993.000 | 0.000 | 7.000 | 7.431 | 1.486 | 6.000 | Detailed Re |
| Bax | 1997 | 0.000 | 0.000 | 1986.000 | 0.000 | 11.000 | 15.347 | 18.444 | 6.000 | Detailed He |
| Produs_finit | 91 | 91.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.027 | 0.700 | 6.000 | Constant labor |
| Bax01 | 1948 | 0.000 | 0.000 | 1943.000 | 0.000 | 5.000 | 13.166 | 16.221 | 6.000 | Circup sobs |
| Folie01 | 12000 | 0.000 | 0.000 | 1948.000 | 0.000 | 10052.000 | 5028.047 | 1005.609 | 6.000 | - Reporting Mo |
| Sticla_etic | 11695 | 0.000 | 0.000 | 11688.000 | 0.000 | 7.000 | 6.377 | 1.309 | 6.000 | As Specifie |
| Elichete01 | 12000 | 0.000 | 0.000 | 11695.000 | 0.000 | 305.000 | 159.405 | 31.881 | 6.000 | |
| Sticla_cu | 11701 | 0.000 | 0.000 | 11695.000 | 0.000 | 6.000 | 5.842 | 1.198 | 6.000 | Group |
| Dopuri01 | 12000 | 0.000 | 0.000 | 11701.000 | 0.000 | 299.000 | 153.562 | 30.712 | 6.000 | |
| Sticla_etic | 11695 | 0.000 | 0.000 | 11688.000 | 0.000 | 7.000 | 6.377 | 1.309 | 6.000 | |
| Bichete02 | 12000 | 0.000 | 0.000 | 11695.000 | 0.000 | 305.000 | 159.405 | 31.881 | 6.000 | |
| Sticle01 | 11708 | 0.000 | 0.000 | 11701.000 | 0.000 | 7.000 | 7.221 | 1.480 | 6.000 | |
| Sticla_cu | 11701 | 0.000 | 0.000 | 11695.000 | 0.000 | 6.000 | 5.842 | 1.198 | 6.000 | |
| Dopuri02 | 12000 | 0.000 | 0.000 | 11701.000 | 0.000 | 299.000 | 153.562 | 30.712 | 6.000 | |
| Sticle02 | 11708 | 0.000 | 0.000 | 11701.000 | 0.000 | 7.000 | 7.221 | 1.480 | 6.000 | |

Fig. 12. Product report.

Product report

After simulating the flow for 5 days (8 hours a day), following the report in Fig. 12, the result was 34944 bottles, 5824 cases, and 91 pallets (finished product) with 64 cases. Therefore, the production increased by 758.3% compared to the production presented in the initial flow.

Production systems report

In the case of the production systems, after simulating the flow working for 5 days, the functioning time was optimised after proper redesigning and parametrising. This applies to the specific flow area for packing the bottles and palletising the cases, as shown in Figs. 13 and 14.

It is noticeable that, during the initial flow, the palletising system only worked at 1.5% of the total production time, as opposed to 11.37% after the optimisation.

Conveyor transport systems report

Regarding the conveyor transport systems used in the bottling flow, the results obtained after simulating and parametrising the conveyors in compliance with the production systems are presented in Figs. 15 and 16.

| Name | % Idle | % Busy | % Filling | % Emptying | % Blocked | % Cycle Wait Labor | % Setup | % Setup Wait Labor | % Broken Down | % Repair Wait Labor | No. (Operat |
|-------------|--------|--------|-----------|------------|-----------|-----------------------|---------|-----------------------|------------------|------------------------|-----------------|
| Imbuteliere | 55.008 | 44.992 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Dopuire | 50.029 | 49.971 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Etichetare | 0.104 | 99.896 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Ambalare | 83.358 | 16.642 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| Paletizare | 88.625 | 11.375 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| Transport | 98.104 | 1.896 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| Robot | 50.000 | 50.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Ambalare01 | 83.767 | 16.233 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| Etichetare | 2.540 | 97.460 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Dopuire01 | 51.246 | 48.754 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Imbutelier | 56.106 | 43.894 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Ambalare02 | 83.767 | 16.233 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | |
| Robot01 | 51.218 | 48.782 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Etichetare | 2.540 | 97.460 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Dopuire02 | 51.246 | 48.754 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Imbutelier | 56.106 | 43.894 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |
| Robot02 | 51.218 | 48.782 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 1 |

Fig. 13. Production systems report.



Fig. 14. Production systems chart.

🗂 Part 🥔 Machine 🛄 Conveyor 🏦 Buffer 🧕 Labor 🗴 Variable

| Name | % Empty | % Move | % Blocked | % Queue | % Broken Down | Now On | Total On | Avg Size | Avg Time |
|------|---------|--------|-----------|---------|------------------|--------|----------|----------|----------|
| C12 | 15.160 | 7.870 | 0.000 | 76.970 | 0.000 | 1 | 1948 | 1.955 | 2.408 |
| C1 | 0.004 | 99.996 | 0.000 | 0.000 | 0.000 | 2 | 12000 | 1.990 | 0.398 |
| C2 | 0.025 | 99.975 | 0.000 | 0.000 | 0.000 | 4 | 11998 | 3.992 | 0.799 |
| C3 | 0.062 | 88.608 | 0.000 | 11.330 | 0.000 | 5 | 11993 | 5.013 | 1.003 |
| C4 | 0.112 | 98.581 | 0.000 | 1.307 | 0.000 | 3 | 11987 | 2.987 | 0.598 |
| C5 | 24.820 | 15.319 | 0.000 | 59.860 | 0.000 | 3 | 1997 | 1.810 | 2.175 |
| C6 | 99.242 | 0.758 | 0.000 | 0.000 | 0.000 | 0 | 91 | 0.008 | 0.200 |
| C7 | 51.727 | 27.424 | 0.000 | 20.849 | 0.000 | 0 | 1948 | 0.633 | 0.780 |
| C8 | 0.112 | 99.220 | 0.000 | 0.668 | 0.000 | 3 | 11695 | 2.917 | 0.599 |
| C9 | 0.062 | 94.191 | 0.000 | 5.747 | 0.000 | 5 | 11701 | 4.868 | 0.998 |
| C10 | 0.025 | 99.975 | 0.000 | 0.000 | 0.000 | 4 | 11705 | 3.894 | 0.799 |
| C13 | 0.112 | 99.220 | 0.000 | 0.668 | 0.000 | 3 | 11695 | 2.917 | 0.599 |
| C11 | 0.004 | 99.996 | 0.000 | 0.000 | 0.000 | 2 | 11707 | 1.912 | 0.392 |
| C14 | 0.062 | 94.191 | 0.000 | 5.747 | 0.000 | 5 | 11701 | 4.868 | 0.998 |
| C15 | 0.025 | 99.975 | 0.000 | 0.000 | 0.000 | 4 | 11705 | 3.894 | 0.799 |
| C16 | 0.004 | 99.996 | 0.000 | 0.000 | 0.000 | 2 | 11707 | 1.912 | 0.392 |

Fig. 15. Conveyor transport systems report.



Fig. 16. Conveyor chart.

Costs report

The analysis of the bottling flow is even more important when considering the production costs.

After the optimisation, the results drastically changed. If the initial profit was 11,704.90\$, after optimisation, the profit reached a value of 57,900.20%, resulting in an increase of 494.66% compared to the initial flow (Fig. 17).

| Revenues | Element | | | By Quantity | Total | Print |
|-------------------------|----------|------------|--------|-------------|---------------|---------------|
| | Parts | | | \$22,750.00 | \$22,750.00 | Cost |
| Total Revenue | | | | \$22,750.00 | \$22,750.00 | |
| | | | | | | Show |
| | | | | | | By Type |
| Costs | Element | Fixed | By Use | By Quantity | Total | O By Group |
| | Pada | 00.00 | | \$14 760 00 | £14 760 00 | By Individual |
| | Machines | \$1 200.00 | \$0.00 | \$64,330,20 | \$65,530,20 | Show All |
| | Labor | \$360.00 | \$0.00 | 004,000.20 | \$360.00 | |
| Total Cost | | \$1,560,00 | \$0.00 | \$79,090,20 | \$80,650,20 | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | brsion E |
| Profits | | | | | | |
| Profits Profit Total | | | | | (\$57,900.20) | - |

Fig. 17. Costs report.

4. SIMULATION USING THE KUHN ALGORITHM

Next up, a complementary simulation method for the intended flow was used, called the Kuhn mathematical algorithm.

Five bottling systems were compared for this stage, four of which already existed on the market and had similar characteristics and work times as presented in Table 1, respectively, the concept system offered by the authors. The data used for the concept system was taken from the reports generated following the simulation in Witness. The reports are explained in the earlier chapter for the 1.5-litre PET bottle.

Kuhn's algorithm uses the following property: the set of minimal solutions of an affect problem does not change if the same real number is added to all elements of a row or column of the cost matrix. Kuhn's algorithm is also based on the fact that a solution to the affected problem corresponds to a coupling of the bipartite graph and proceeds in several steps [9].

The following conventions are adopted for transposing the language of graph theory in matrix terms:

- A line or column is considered covered if, at a certain step, it is part of the set of marked nodes in the process of determining minimum support.
- An array element is considered circled if it is part of the coupling found up to that point.
- An element of the matrix is said to be cut if it corresponds to an edge that can be used to obtain a growth path, in a sense that will be clarified later.

Several stages will be completed respecting the previously presented conventions to validate the most efficient option for bottling, including bottling in 1.5-litre PET bottles using Kuhn's algorithm.

In this sense, the data related to the production time for the 5 bottling systems: MITSUBISHI ELECTRIC (ME), KRONES (KR), CONCEPT (CO), ACASI MACHINERY (AM), SMIGROUP (SM), in correspondence with the bottles PET of 0.5 litres; 1 litre; 1.5 litres; 2 litres and 2.5 litres was collected. Identification of the most efficient system for bottling liquid in PET containers is necessary in order to minimise the execution time of this activity.

The total time for the bottling process, stated in minutes, specific to each flow for making 10 cases of 6 bottles of every type, is represented in Table 1

Step 1. The lowest element is chosen from each line(the minor) that will t be extracted from the other elements (Table 2).

Step 2. The procedure is repeated, this time from each column, subtracting the lowest element from the other elements (Table 3).

Step 3. The rows and columns are scanned one by one. On the first row, there is only one element 0, and a vertical line is drawn on column 5; on the second row, there is only one element 0, and a vertical line is drawn on column 2; on the third row, there is only one element 0 and a vertical line drawn on column 3, on the fourth row there is only one element 0, but it was previously cut, and on the fifth row there are two zeros, and we leave it be. The same procedure is done for the columns (Table 4).

Table 1

Specific time for the bottling operation

| Cases type System | ME | KR | СО | AM | SM |
|----------------------|----|----|----|----|----|
| Cases 0.5 l | 60 | 69 | 55 | 70 | 50 |
| Cases 1.01 | 64 | 55 | 75 | 70 | 60 |
| Cases 1.5 l | 56 | 50 | 48 | 60 | 56 |
| Cases 2.01 | 68 | 48 | 50 | 60 | 50 |
| Cases 2.5 l | 50 | 69 | 55 | 60 | 60 |

Table 2

| age I | |
|-------|--|
|-------|--|

St

| Cases type System | ME | KR | СО | AM | SM |
|----------------------|----|----|----|----|----|
| Cases 0.5 l | 10 | 19 | 5 | 20 | 0 |
| Cases 1.0 l | 9 | 0 | 20 | 15 | 5 |
| Cases 1.5 l | 8 | 2 | 0 | 12 | 8 |
| Cases 2.0 1 | 20 | 0 | 2 | 12 | 2 |
| Cases 2.5 1 | 0 | 19 | 5 | 10 | 10 |

Table 3

| | | Stag | C 2 | | |
|----------------------|----|------|-----|----|----|
| Cases type System | ME | KR | СО | AM | SM |
| Cases 05 1 | 10 | 19 | 5 | 10 | 0 |
| Cas.es 1,01 | 9 | 0 | 20 | 5 | 2 |
| Cases 1.51 | 8 | 2 | 0 | 2 | 5 |
| Cases 2.0 1 | 20 | 0 | 2 | 2 | 2 |
| Cases 2.5 1 | 0 | 19 | 5 | 0 | 4 |

Stano 2

Table 4

| | Stage 3 | | | | | | | | | |
|----------------------|---------|----|----|----|----|--|--|--|--|--|
| Cases type System | ME | KR | СО | AM | SM | | | | | |
| Cases 0.5 1 | 10 | 19 | 5 | 10 | 0 | | | | | |
| Cases 1.01 | 9 | 0 | 20 | 5 | 2 | | | | | |
| Cases 1.5 l | 8 | 2 | 0 | 2 | 5 | | | | | |
| Cases 2.01 | 20 | 0 | 2 | 2 | 2 | | | | | |
| Cases 2.51 | 0 | 19 | 5 | Û | 4 | | | | | |

Table 5

Step 4. We checked the requirement and noticed that the number of rows (5) and repartitions (4) were not fulfilled. We are looking to obtain the maximum coupling and move on to the next stage (Table 4).

STEP 5. We search for the minor of the uncut boxes. The element will be = 2.

STEP 6. The minor of the uncut boxes, which is two, is added to the double-cut elements; it is subtracted from the uncut elements, and elements cut with one line are left unchanged. The following matrix is obtained (Table 5).

| Cases type System | ME | KR | СО | AM | SM |
|----------------------|------------|----|----|----|----|
| Cases 0.5 l | 8 | 19 | 5 | 8 | 0 |
| Cases 1.01 | 7 | 0 | 20 | 3 | 2 |
| Cases 51 | 6 | 2 | 0 | 0 | 5 |
| Cases 2.01 | 18 | 0 | 2 | () | 2 |
| Cases 2.5 l | \bigcirc | 21 | 7 | 0 | 6 |

Stages 6 and 7

STEP 7. On the first line, there is only one 0 that we circle and then cut column 5. On the second line there is also only one 0 that we circle and then cut the second column. On line 3, there are two zeros, and we leave it be. On the fourth line, there is only one 0 left, the other being previously cut. On line 5, there is also only one 0 left, the other one being previously cut, and we cut the given column. The same procedure is done with the columns. The only column that has a 0 and is left uncut is the third one. The same procedure is followed. The 0 on that column is circled, and the third row is cut with a horizontal line.

STEP 8. The condition that the number of rows (5) and the number of repartitions (5) is checked, the requirement is fulfilled in this case. We got the maximum coupling [11].

The algorithm indicates that the most lucrative bottling system is the one suggested by the authors for the 1.5-litre bottles.

5. CONCLUSION

A water bottling process was simulated using the KUHN mathematical algorithm and the WITNESS Horizon software to maximise production efficiency.

Upon optimising the workflow by adjusting the working hours and adding two more bottling lines, the proposed objective of increasing profit was achieved. During the initial parameterisation, it was noted that the palletising system was operating at only 1.5% efficiency. After optimisation, this increased to 11.37% compared to the initial flow parameterisation.

After analysing the optimised system, it was observed that production increased by 758.3% compared to the initial flow variant. This resulted in 34944 PET bottles (compared to 4801 bottles in the initial simulation), 5824 boxes (compared to 794 boxes in the initial simulation), and 91 "finished product" pallets (compared to 12 pallets in the initial simulation).

The present study used a complementary method to confirm the results obtained for the proposed flow. Specifically, four bottling systems from different companies that create a complete flow were selected. Following the selection, the systems were simulated using the method proposed by the CONCEPT authors in WITNESS Horizon. Upon completing the specific stages of the Kuhn algorithm, the bottling system configuration proposed by the authors was further validated. It was confirmed that maximum efficiency is achieved when bottling in 1.5-litre PET bottles.

REFERENCES

- [1] M.L. Boca, P. Kovač, and B. Savković, Model Approch of Automation of Bottling and Packaging for Industrial Process of Bottles, Vol. 20, No. 2, 2017, University of Novi Sad, Faculty of Technical Sciences, Institute for Production Engineering, Novi Sad, Serbia.
- [2] Shemesh Automation.Automated Packaging Machinery, https://www.shemeshautomation.com/, accessed 02 October 2023.
- [3] Krones, Solutions beyond tomorrow, https://www.krones.com/en/index.php, accessed 02 October 2023.
- [4] C.L. Popa, C.E. Cotet, Virtual Model in Monitoring and Optimization of a Selective Waste Collection Integrated System, Proceedings of the 5th International Conference on Advanced Manufacturing Engineering and Technologies—NEWTECH 2017, Belgrade, Serbia, 5–7 June 2017, pp. 41–55.
- [5] C. Liu, and M. Lee, Integration, supply chain resilience, and service performance in third-party logistics providers, Int. J. Logist. Manag, Vol. 29 No. 1, 2018, pp. 5–21.
- [6] H. Zhang, Z. Wang, X. Hong, Y. Gong, & Q. Zhong, Fuzzy closed-loop supply chain models with quality and marketing effortdependent demand, Expert Systems with Applications, 207, (2022),118081.
- [7] J. Ong, M. Latif, & S. Kundu, *Exploiting Witness Simulation for SCM*, International Journal of Research in Management, Science & Technology, Vol. 2, Issue 2, 2014, pp. 103–109.
- [8] M.V.K. Shinde and U.M. Nimbalkar, *Review on manufacturing predictive simulation: Use of WITNESS simulation software*, International Journal of Scientific & Engineering Research, Vol. 8, Issue 4, April-2017, pp. 355–358.
- [9] H. Kuhn, The Hungarian method for the assignment problem, Nav. Res. Logist., 2, 1955, pp. 83–97.
- [10] R. Fletcher, Conjugate Gradient Methods for Indefinite Systems, Lecture Notes in Math, Springer, Berlin/Heidelberg, Germany, Vol. 506, 1976, pp. 73–89.
- [11] A. Bjorck, Numerical Methods for Least Squares Problems, SIAM Publisher: Philadelphia, PA, USA, 1996.